

USING TRIG IDENTITIES
By Chris I

Ya, I feel you.

BRACE YOURSELF



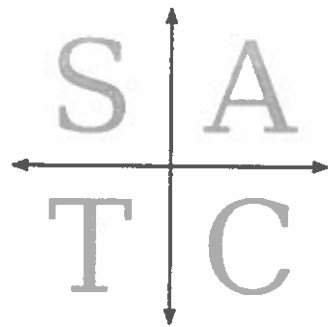
So here are the basic ideas that you want to
Memorize if you even want a chance
With these identities:

$$\begin{aligned}\sin^2x + \cos^2x &= 1 \\ \tan x &= \sin x / \cos x \\ \sec x &= 1 / \cos x \\ \sin^2x &= 1 - \cos^2x\end{aligned}$$

$$\tan^2x + 1 = \sec^2x$$

$$\csc x = 1 / \sin x$$

$$\begin{aligned}\cot^2x + 1 &= \csc^2x \\ \cot x &= \cos x / \sin x \\ \cot x &= 1 / \tan x \\ \cos^2x &= 1 - \sin^2x\end{aligned}$$



Quadrant 1: All trig functions are +

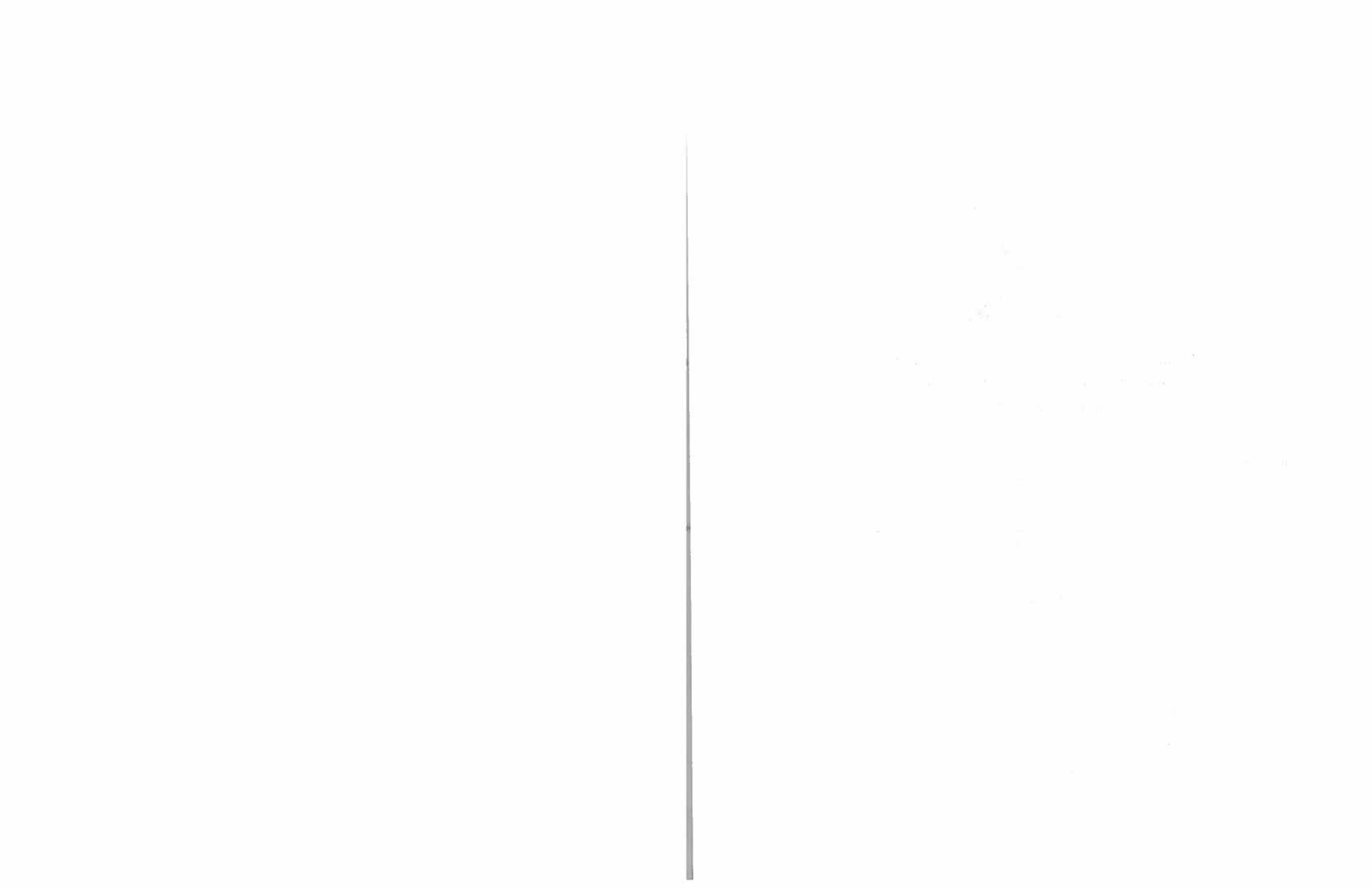
Quadrant 2: Sine is +

Quadrant 3: Tangent is +

Quadrant 4: Cosine +

Remember: All Students Take Calculus

These ideas are pretty straight forward. Just understand when trying to tackle a problem, this is what you need to succeed in the end! I mean, ya, they look easy now... JUST WAIT!
HAHAHAHAAHAHAHAHAHAHAHA. No? Not funny? Ok....



1. Given $\sin x = 2/5$, and $\frac{\pi}{2} < x < \pi$. Find the values of the other five trig functions.



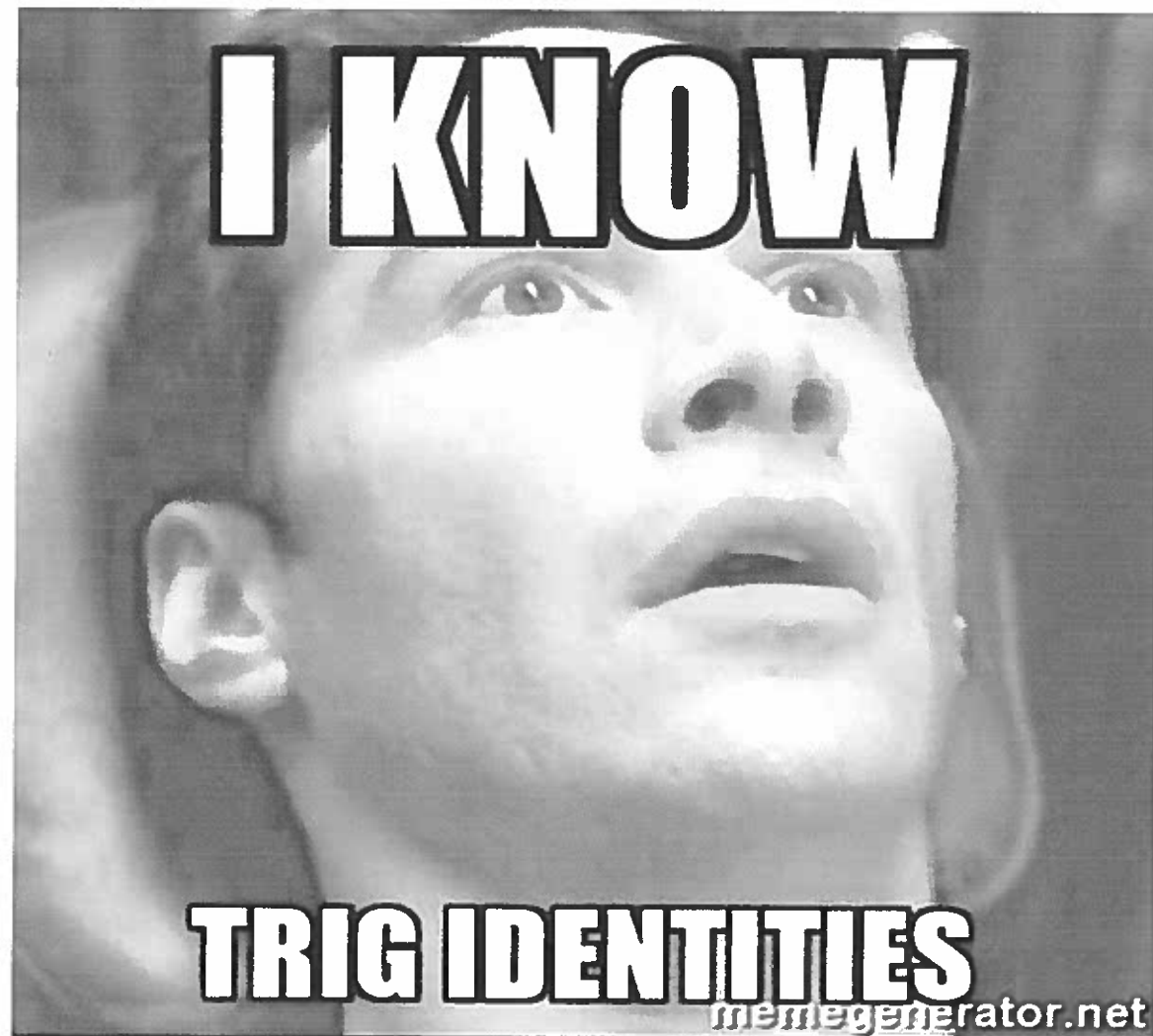
Yes I understand 3 is not half of 5 but its close enough

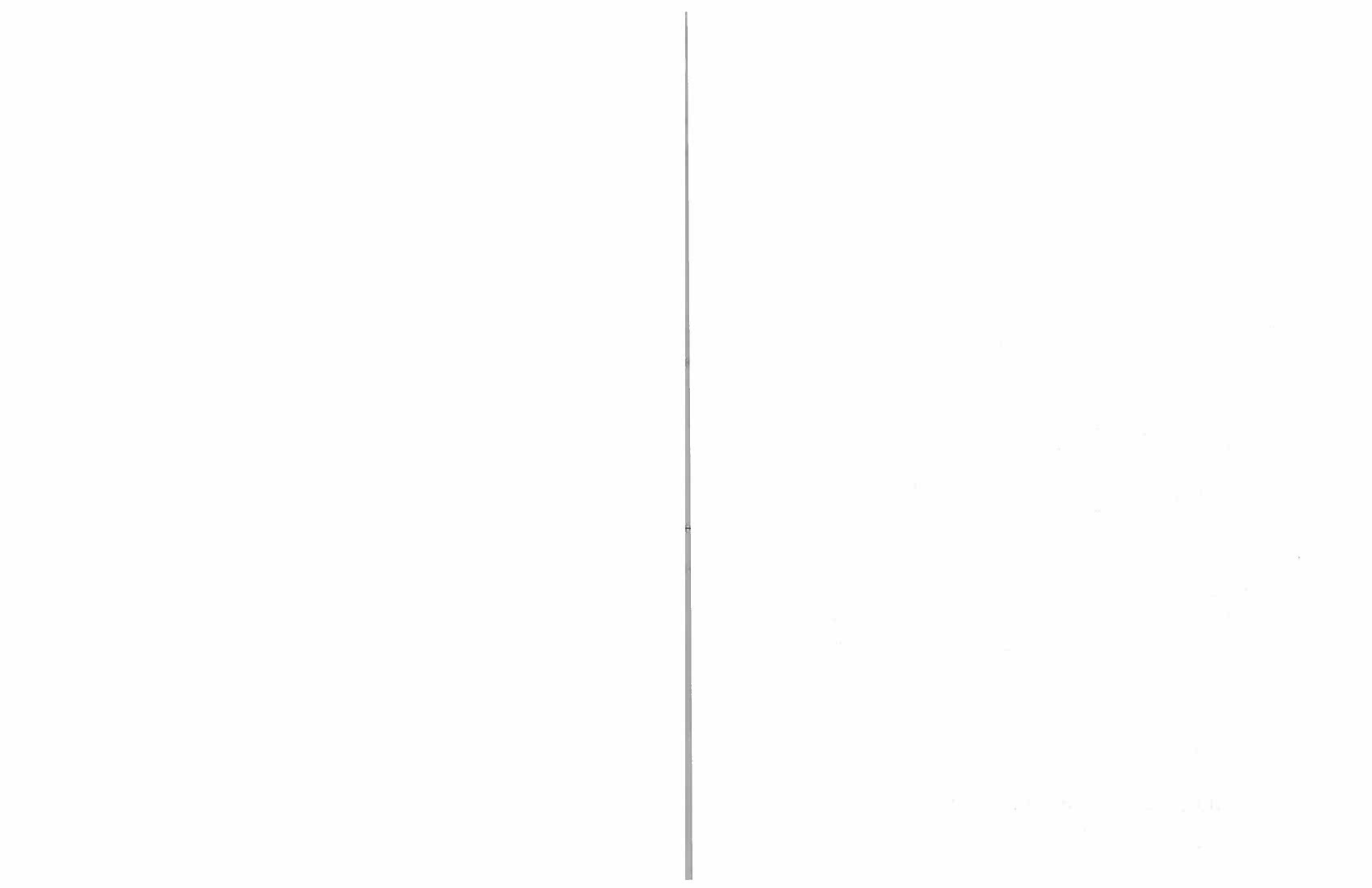
2. $\tan A + \cot A = \sec A \csc A$



5. $\frac{\sin x \cot x + \cos^2 x}{1 + \cos x} = \cos x$

CONGRATS YOUNG PADWAN. You have successfully been terribly taught by yours truly to understand and know Trig Proofs. Now, you will pass this final and be really cool. Duh. Hope you enjoyed my great memes.





Answers:

Question 1: Given $\sin x = 2/5$, and $\frac{\pi}{2} < x < \pi$. Find the values of the other five trig functions.

$$\sin^2 x + \cos^2 x = 1$$

$$(2/5)^2 + \cos^2 x = 1$$

$$4/25 + \cos^2 x = 1$$

$$-4/25 \quad -4/25$$

$$\sqrt{\cos^2 x} = \sqrt{21/25} \quad 21/25 = .84 \quad 2/5 = .4$$

$$\cos x = \pm .917$$

$$\cos x = -.917 \leftarrow \text{It's in Quad II}$$

Now for the rest...

$$\tan x = \sin x / \cos x \quad .4 / -.917 = -.436 \quad \sec x = 1 / \cos x \quad 1 / -.917 = -1.09$$

$$\csc x = 1 / \sin x \quad 1 / .4 = 2.5 \quad \cot x = \cos x / \sin x \quad -.917 / .4 = -2.29$$

Question 2: $\tan A + \cot A = \sec A \csc A$

$$\frac{\sin A}{\cos A} + \frac{\cos A}{\sin A}$$

$$\frac{\sin A \times \sin A}{\sin A \times \cos A} + \frac{\cos A \times \sin A}{\sin A \times \cos A}$$

$$\frac{\sin^2 A + \cos^2 A}{\sin A \cos A} \rightarrow \frac{1}{\sin A \cos A} \rightarrow \sec A \csc A = \sec A \csc A$$

Question 3: $\sin^2 x (1 + \tan^2 x) = \tan^2 x$

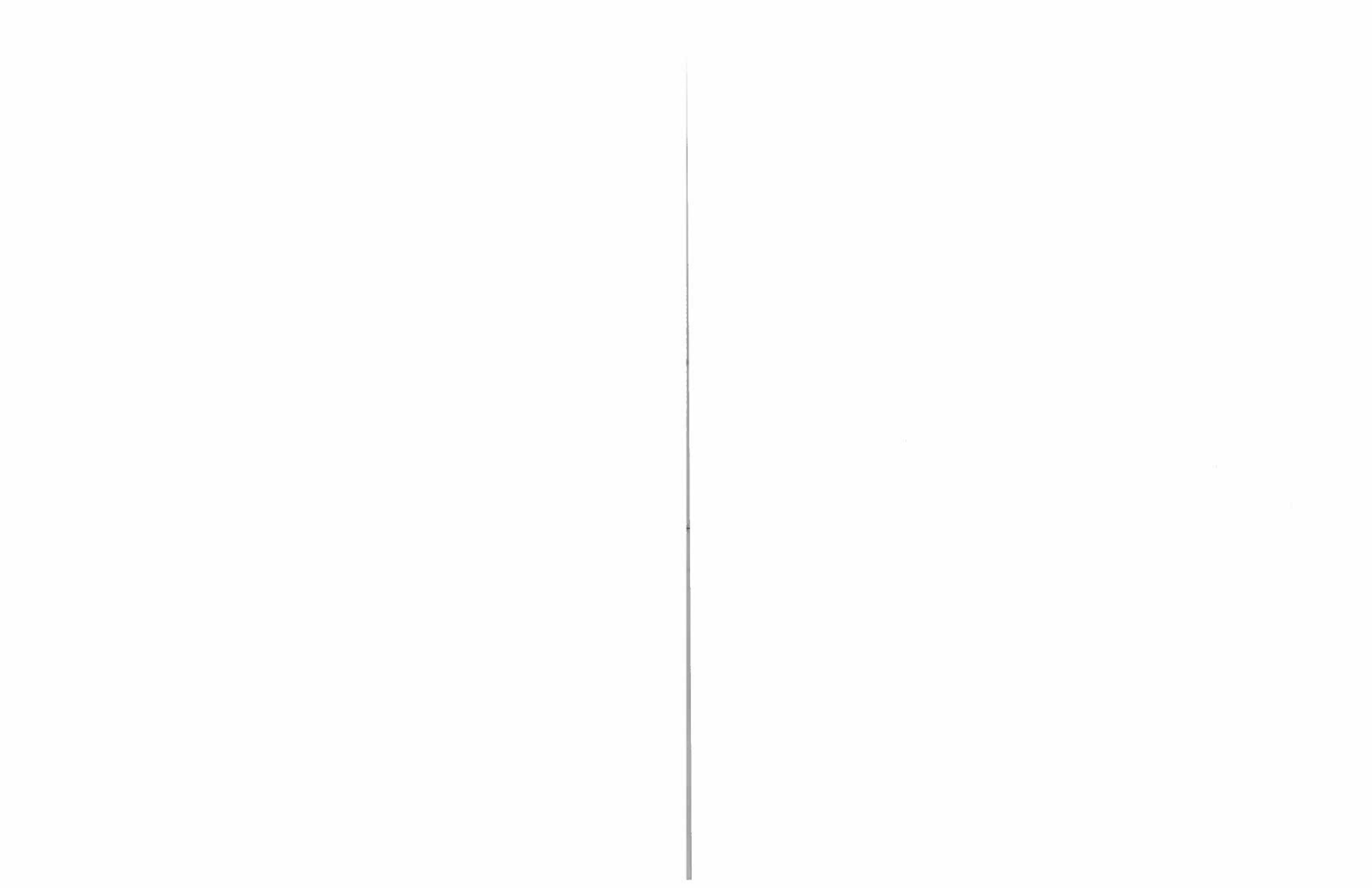
$$\sin^2 x (\sec^2 x) \rightarrow \sin^2 x \left(\frac{1}{\cos^2 x} \right)$$

$$\frac{\sin^2 x}{\cos^2 x} \rightarrow \tan^2 x = \tan^2 x$$

Question 4: $\frac{\cos x \sin 2x}{1 - \cos x} = \cos x + \cos^2 x$

$$\frac{\cos x (1 - \cos^2 x)}{1 - \cos x} \rightarrow \frac{\cos x (1 - \cos x)(1 + \cos x)}{1 - \cos x}$$

$$\cos x (1 + \cos x) \rightarrow \cos x + \cos^2 x = \cos x + \cos^2 x$$



Question 5: $\frac{\sin x \cot x + \cos^2 x}{1 + \cos x} = \cos x$

$$\frac{\sin x \frac{\cos x}{\sin x} + \cos^2 x}{1 + \cos x} \rightarrow \sin \frac{\cos}{\sin}$$

$$\frac{\cos + \cos^2 x}{1 + \cos x} \text{ And then } \frac{\cos x(1 + \cos x)}{1 + \cos x}$$

$$\cos x = \cos x$$

